

The plan of the future study (Shigeyasu KAMIYA)

As mentioned in “The results of my studies,” it is important to investigate complex hyperbolic triangle groups, so I will continue this research.

Specifically, I will proceed to study the following problems.

- 1) Our list of groups of type $(n, n, \infty; k)$ is not complete yet, so this should be completed.
 - a) To construct new complex hyperbolic versions of Jorgensen’s inequality as criteria for a group to be discrete.
 - b) To make our “old” complex hyperbolic versions of Jorgensen’s inequality more precise ones.
 - c) To find out a criterion for a group to contain a Fuchsian subgroup.
 - d) To generalize the result on Diophantine equations by Conway and Jones.
 - e) To consider some criteria for arithmeticity of a group.
 - f) To find a new method for constructing fundamental domains.
 - g) To study how the properties of a group are changed when generators are transferred to different ones by certain isomorphisms.
 - h) Given a discrete complex hyperbolic triangle group G . To discuss the difference between this group G and a group, which is “close” to G in the parameter space.
 - i) To compare complex hyperbolic triangle groups with real ones by studying the construction of arithmetic triangle groups acting on the real hyperbolic space,
 - j) To find discrete groups and construct their fundamental domains
 - k) To find out non-arithmetic complex hyperbolic triangle groups.
- 2) To do the same problems as above in complex hyperbolic triangle groups of type (n, n, ∞) , which are not expressed as $(n, n, \infty; k)$. To construct fundamental domains for these discrete groups, because these groups seem to be discrete.
- 3) To study complex hyperbolic triangle groups of general type (p, q, r) .
- 4) To find some relations between complex hyperbolic triangle groups and automorphic functions on complex hyperbolic space.