Summary of Research Noriyuki Hamada

My main research interest is low dimensional topology, especially, study of *smooth* 4-*manifolds* via *mapping class groups of surfaces*. More specifically, finding new *Lefschetz pencils* with various interesting features has been my greatest contributions to the research area and I take pride in having distinguished skills to construct Lefschetz pencils from the combinatorial aspect in terms of mapping class groups. Lefschetz pencils can be regarded a topological description of symplectic manifolds, hence my interest naturally extends to 4-*dimensional symplectic topology*, and also to 3-*dimensional contact topology* (as the boundaries of symplectic 4-manifolds).

Lefschetz pencils were originally introduced to study topological aspects of nonsingular projective varieties, so *holomorphic* Lefschetz pencils had been of classical interest. However, it revealed in the late 1990s that there is an excellent correspondence between Lefschetz pencils and *symplectic manifolds*, and since then this fact has become the strongest motivation to study Lefschetz pencil structures. Namely, the following fundamental theorem holds: a closed manifold admits a symplectic structure if and only if it admits a Lefschetz pencil structure. From this fact, we can study symplectic manifolds via Lefschetz pencils.

I have mainly worked to <u>construct explicit Lefschetz pencils on basic symplectic 4-</u> <u>manifolds or construct Lefschetz pencils (or Lefschetz fibrations) with interesting features</u>. In the paper [1], I studied the minimal numbers of singular fibers in Lefschetz fibrations over the tori, and gave pretty good upper bounds for them. The paper [2] investigates holomorphic Lefschetz pencil structures on the four-torus with great details. The preprint [3] presented systematic constructions of various examples of non-holomorphic Lefschetz pencils. In [4], I elaborately studied the pencil structures of one of the most basic Lefschetz fibrations called the Matsumoto-Cadavid-Korkmaz Lefschetz fibration and gave various Lefschetz pencils. In [5], I discovered much simpler expressions for the well-known genus-1 Lefschetz pencils.

References

- N. Hamada, Upper bounds for the minimal number of singular fibers in a Lefschetz fibration over the torus, Michigan Math. J. 63 (2014), 275--291.
- [2] N. Hamada and K. Hayano, Topology of holomorphic Lefschetz pencils on the four-torus, Algebr. Geom. Topol. 18 (2018), no. 3, 1515–1572.
- [3] N. Hamada, R. Kobayashi and N. Monden, Non-holomorphic Lefschetz fibrations with (-1)sections, to appear in Pacific J. Math.; also available at https://arxiv.org/abs/1609.02420.
- [4] N. Hamada, Sections of the Matsumoto-Cadavid-Korkmaz Lefschetz fibration, preprint; https://arxiv.org/abs/1610.08458
- [5] N. Hamada, Simple expressions for the holed torus relations, preprint(2017); https://arxiv.org/abs/1701.02171.