

# Research program

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The following researches are projected.

- **Cable versions of the  $\Gamma$  and Jones polynomials**

I will study the problem “Which is strong, cable version of the  $\Gamma$ -polynomial or cable version of the Jones polynomial?”

- **The  $(p, q)$ -cable version of the  $\Gamma$ -polynomial for sufficiently large  $p$**

Considering the  $(p, q)$ -cable version of the  $\Gamma$ -polynomial for sufficiently large  $p$ , I will study whether we can obtain geometric information of knots like the volume conjecture.

- **Kawauchi’s conjecture**

Let  $K, K'$  be knots. If  $\Gamma_{p/q}(K) = \Gamma_{p/q}(K')$  for any coprime integers  $p(> 0)$  and  $q$ , then  $P(K) = P(K')$  and  $F(K) = F(K')$ , where  $\Gamma_{p/q}$  is the  $(p, q)$ -cable version of the  $\Gamma$ -polynomial,  $P$  is the HOMFLYPT polynomial and  $F$  is the Kauffman polynomial.

- **Cable version of the first coefficient HOMFLYPT polynomial for mutant knots**

It was shown that cable version of the zeroth coefficient HOMFLYPT polynomial, that is, the  $\Gamma$ -polynomial is invariant under mutation by Tetsuya Ito. Our interest is the case of cable version of the first coefficient HOMFLYPT polynomial.

- **Relation between the  $\Gamma$ -polynomial, its  $(2, 1)$ -cable version, HOMFLYPT and Kauffman polynomials**

We have already shown that there exist infinitely many knots with the trivial  $(2, 1)$ -cable version of the  $\Gamma$ -polynomial and the knots have the trivial  $\Gamma$ -polynomial and the trivial first coefficient HOMFLYPT and Kauffman polynomials. I consider whether any knot with the trivial  $(2, 1)$ -cable version of the  $\Gamma$ -polynomial has the trivial  $\Gamma$ -polynomial and the trivial first coefficient HOMFLYPT and Kauffman polynomials.

- **Characterization of the  $\Gamma$ -polynomials of knots by using knots with clasp number at most two**

It is known that the  $\Gamma$ -polynomials of knots are characterized by using 2-bridge knots with unknotting number one. I consider whether the  $\Gamma$ -polynomials of knots can be characterized by using knots with clasp number at most two.

- **Clasp-pass moves of type  $X$  and the  $\Gamma$ -polynomial for knots**

It is known that the  $\Gamma$ -polynomial is invariant under clasp-pass moves of type  $X$ . I consider whether  $\Gamma(K) = \Gamma(K') \Rightarrow K \sim_{CPX} K'$ .

- **Minimal grid diagrams and minimal closed braid diagrams**

(Joint work with Hwa Jeong Lee)

Every knot has minimal grid diagrams. We consider whether there always exists a minimal grid diagram which presents a minimal closed braid diagram.