# **Research proposal**

## Mitsuyo Suzuki

The applicant has conducted research in particle physics, with a focus on supersymmetry and gradient flow. This research relates to various topics including renormalization, numerical calculations, string theory, and AdS/CFT correspondence. In addition to continuing the previous research described in the attached sheet, the applicant is interested in exploring other areas of research as well.

# Supersymmetric Gradient Flow in SQCD

In previous work, we examined the perturbation theory and divergence structure of supersymmetric gradient flow in four-dimensional  $\mathcal{N} = 1$  supersymmetric quantum chromodynamics (SQCD) [1]. However, this investigation was limited to the one-loop level for two-point functions in the Wess-Zumino gauge. In the case of Yang-Mills flow, it is shown that UV-divergences are absent in any flowed correlation function at all orders of perturbation theory. We aim to prove the result of [1]. Additionally, while the Wess-Zumino gauge does not preserve manifest supersymmetry, the results of [1] suggest that manifest supersymmetry is recovered. As a further study, it would be interesting to explore the perturbation theory using the superfield formalism, a supersymmetric gauge-fixing, and different regularization schemes.

#### Numerical Applications in SQCD

One notable aspect of gradient flow is the ability to derive new gauge-invariant physical quantities using the UV-finiteness and small flow time expansion. This enables the examination of physical quantities obtained with different regularization schemes. We aim to formulate observables using SQCD flow , and to apply this to numerical calculations.

## Other applications and extension of supersymmetric flow

Gradient flow has also been applied in the study of the AdS/CFT correspondence, which claims a profound relationship between a *D*-dimensional conformal field theory and a (D + 1)-dimensional supergravity theory. In an attempt to understand the correspondence from a different perspective, a method for defining the geometry of (D + 1)-dimensions from *D*-dimensional gauge theories using gradient flow equations has been proposed.

Another area of interest is the construction of an exact renormalization group (ERG) which is manifestly gauge-invariant. While the ERG provides a framework for studying quantum field theories beyond perturbation theory, the momentum cutoff makes it difficult to preserve gauge symmetry. The gradient flow can propose a gauge-invariant ERG.

Applying these studies to supersymmetric theories will enhance our understanding of gradient flow and supersymmetry, and facilitate a variety of related applied research. To achieve this, we plan to also work on extending supersymmetric flow theory to  $\mathcal{N} = 2, 4$  supersymmetric theories.