

Research Plan

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I will continue the research for the 2d / 4d (5d, 6d) correspondence and the tensor models

2d/4d(5d,6d) correspondence

As mentioned in the “Research Results”, I have considered the irregular limit of the β - A_{n-1} type multi-matrix model and revealed part of the rich mathematical structure of this model. However, with the currently used method, only two of the $2n$ mass parameters can be taken to the infinity limit and three or more are not possible. This is why in the limit to the $N_f \leq 2n - 3$ models, we face the difficulty that the size of the matrix, which also appears as an important parameter in correspondence with gauge theory, goes to infinity. From the studies so far, it has been suggested that this difficulty could be avoided by applying the appropriate transformation to the matrix model. First, I would like to establish a procedure to realize $N_f = 1$ and $N_f = 0$ in the $su(2)$ model. Also, the generalization to $su(n)$ should be proceeded as well.

On the other hand, I will study the 2d/5d(6d) correspondence, which is an extended version of the 2d/4d correspondence (AGT correspondence) between two-dimensional conformal field theories and four-dimensional supersymmetric gauge theories. The 2d/5d correspondence is obtained by the q -transformation of the 2d/4d correspondence. The 2d/6d correspondence corresponds to the elliptic 2d/5d correspondence.

Extending the research described above, I would like to establish the irregular limit in the q deformed and elliptic models. This limit has never been considered in a q -deformed and elliptic models, and is expected to provide new knowledge and research directions.

Since the q -Virasoro/ W_N algebra appears in the level N representation of Ding-Iohara-Miki (DIM) algebra, it is considered that the DIM algebra plays an important role behind the 2d/5d connection. There is also a known prescription for extending to elliptic DIM algebra, which can be used to extend to 2d/6d correspondence. I will clarify the role of the (elliptic) DIM algebra and establish the understanding of the 2d/6d correspondence. It is expected that the 2d/4d(5d) correspondence can be understood as a special limit of the 2d/6d correspondence. In addition, I would like to clarify the whole picture, including the root of unity limit which I have established in the past studies.

Tensor model

The tensor model appears as a natural extension of the matrix model. The tensor model has received much attention in relation to the low-dimensional AdS/CFT correspondence and further research is desired. I have been studying non-trivial sets of gauge -navariant operators in tensor models by using Op/FD/dessin correspondence and generalized cut operation. Here the dessin is a graph embedded on a two-dimensional surface and has geometric meaning, corresponding to triangulation of the surface. On the other hand, the cut operation generates other operators from one operator and it is also the basic element that constitutes the Virasoro constraint together with join operation. As mentioned in “Research Result”, the efforts of the cut & join operations on dessins are clarified by the Op/dessin correspondence. Its two-dimensional geometric meaning was also revealed. I would like to utilize these results for deepening our knowledge of the Virasoro constraint of the tensor model.

Since the correspondence with dessin is limited to the rank 3 tensor model, I will explore the possibility of the extension to general ranks.