My Results

My result I have published is master thesis of my own written in 1991. So I explai here the thesis "HausdorÆimension and Self-similar set" .

The thesis has an expository part dealing with HausdorÆmension and self-similar sets. They are very useful techquics in Fractal Geometry. It also has explanations of some preliminaries and one of the newest result about self-similar set at that time.

The self-similar sets are built up of pieces geometrically similar to the entire set but on a smaller scale. More accurately, let K be a compact set in a complete metric space X. We call the set K is self-similar, or K has self-similarity if for a \mathfrak{A} te set of contractions $\{S_1, \ldots, S_n\}$ of X, the union $\bigcup_{i=1}^n S_i(K)$ equal to K. Some typical fractals such as Koch curves, Sierpinski gaskets, Cantor sets and so on, are self-similar.

The HausdorÆimension is a quantity representing complexity of a fractal set. The Hausdorf dimension of a subset in the n dimensional Euclidian space is n provided that it has positive Lebesgue measure. In general, Lebesgue measure of fractal set is 0 or ∞ . Accordingly, Lebesgue measure is no use to investigate fractal sets. On the other hand, for each fractal set K, there exists a non-negative real number s such that s dimensional Hausdorll measure has a α te measure on K. This s is the HausdorÆimension of K. It is very important to measure fractal sets.

In general, the HausdorÆimension is hard to calculate. However, Hutchinson shows in his paper of 1981 if the contracions which de sets a self-similar set are compositions of dilation, rotation and translation, and they satisfy "Open set condition", then the HaudorÆimension of the set coincides the similarity dimension. The similarity dimension has advantage of being easily calculable. In Hutchinson's paper, a self-similar set K is de detated as the image of continuous mapping of an Alphbet space. An Alphbet space means a countable product space of $\{1, \ldots, n\}$. Then the main results are derived by using the geometric measure theory in the Alphbet space.

Hanada deals with the case that the contractions are C^1 class in his preprint in 1990. He also makes use fo geometric measure theory in the Alphbet space, in addition ergodic theory and statistical mechanics. Then he shows that the HausdorÆmension can be expressed by a kind of entropy.

My master thesis **\Omega**shes at giving the Hanada's result. When I was the second grade student of Master course at Kyushu University, I tried to improve the results of Hutchinson but I could not. For that reason, the thesis has not original work of mine.