

Program on my study

As I mentioned in the item “About my past research”, my theme has been mainly on the Capelli identities. There are lots of different variations and possibilities to develop on it. I dare say, too many possibilities, and no one could exhaust such theme. We could feel, however, any, though small, possibilities to catch something there. Technical difficulties are in that we treat sort of complicated no-commutativities. Still, in many points, we succeeded in getting non-trivial results.

In the past, I had some hopeful ideas to new results. But, I regret I had no enough time to pursue those ideas. Now, I am hoping to return to face these ideas.

One example is the Capelli identities for the dual pair $(\mathfrak{sp}_{2n}, \mathfrak{o}_m)$. We know that such identities are far from obvious, as M. Itoh calculated. I think, however, other approaches would be hopeful, which idea came to me in 2000. I hope I could restart to pursue this train of thought.

I have other unpublished results on invariant theory, so that I should complete these studies.

Another theme is to investigate the works by Lambert, who lived about 300 years ago. There are lots of interesting things to look at. Among them, his W function is a particular special function, which has many different aspects with applications. Also, Lambert is known as quite a scholar, so that study on him will be fruitful even to the modern time.

What I have proposed are, though scattered in some sense, are possibly unified in a background. It is my experience.

I once read through very old paper by Euler on the pentagonal number theorem, and got a new prospect from it. Also, from a paper by Turnbull, I got a new type of Capelli identities. So, from the Lambert work, I hopefully get something new to us.

Lambert’s work on W function are, deeply related to solution of algebraic equations, apart from the pure “algebraic” approach. From this point of view, a new aspect for what Lagange, Euler, and Galois thought on the algebraic equations, would be obtained, I hope. It is very interesting point of view.