

# “Frontiers in Science” Seminar

## Dr. Piotr Graczyk

**LAREMA, Université d’Angers, France**

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Title : Penalized estimation for Big Data in Regression Problems and its Geometry



Date & Time : April 9, 15:00~16:30

Venue : Sci. Bldg., E408 (Sugimoto C.)

Abstract: It is known that LASSO discovers the sign of the vector  $b$  in the regression equation  $Y = Xb + \varepsilon$ . In the study of Big Data one needs to identify more informative patterns of the vector  $b$ . We define the pattern of any regression estimator with polyhedral penalty. Surprising links between the pattern of a penalized estimator and the geometry of the convex polytope  $B^*$  will be explained. In particular, we study in detail estimation with a sorted  $\ell^1$  penalty, called SLOPE. The SLOPE pattern of a vector  $b$  provides: the sign of its components, clusters (components equal in absolute value) and clusters ranking.



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# Lecture Series "Frontiers in Science"

## Dr. Piotr Graczyk

**LAREMA, Université d'Angers, France**

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Title : Modern Statistical Estimation with a Penalty and its Geometry

Date & Time : April 13, 13:15~14:45

April 16, 13:15~14:45

April 20, 13:15~14:45

Venue : Sci. Bldg., E408 (Sugimoto C.)



We consider the regression problem  $Y = Xb + \varepsilon$  where  $X$  is the matrix with data on  $p$  variables observed  $n$  times,  $Y \in \mathbb{R}^n$  the response vector and  $\varepsilon$  an error. The coefficient vector  $b \in \mathbb{R}^p$  is unknown and must be estimated. In classical statistics we have  $n \geq p$  and we use an Ordinary Least Squares estimator OLS. In modern statistics we need to consider the case  $n < p$  of Big Data. The OLS is then penalized. Surprising links between the pattern discovered by an estimator with a polyhedral penalty  $p$  and the geometry of the  $p^*$ -dual ball  $B^*$  will be explained.

Plan of the lectures: 1. OLS Estimator. 2. LASSO Estimator and its properties.  
3. Estimators with a polyhedral penalty and their properties.



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