

“Frontiers in Science” Seminar

Dr. Piotr Graczyk

LAREMA, Université d’Angers, France

Title : Penalized estimation for Big Data in Regression Problems and its Geometry

Date & Time : April 9, 15:00~16:30

Venue : Sci. Bldg., E408 (Sugimoto C.)



Abstract: It is known that LASSO discovers the sign of the vector b in the regression equation $Y = Xb + \varepsilon$. In the study of Big Data one needs to identify more informative patterns of the vector b . We define the pattern of any regression estimator with polyhedral penalty. Surprising links between the pattern of a penalized estimator and the geometry of the convex polytope B^* will be explained. In particular, we study in detail estimation with a sorted ℓ^1 penalty, called SLOPE. The SLOPE pattern of a vector b provides: the sign of its components, clusters (components equal in absolute value) and clusters ranking.



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Lecture Series "Frontiers in Science"

Dr. Piotr Graczyk

LAREMA, Université d'Angers, France

Title : Modern Statistical Estimation with a Penalty and its Geometry

Date & Time : April 13, 13:15~14:45

April 16, 13:15~14:45

April 20, 13:15~14:45

Venue : Sci. Bldg., E408 (Sugimoto C.)



We consider the regression problem $Y = Xb + \varepsilon$ where X is the matrix with data on p variables observed n times, $Y \in \mathbb{R}^n$ the response vector and ε an error. The coefficient vector $b \in \mathbb{R}^p$ is unknown and must be estimated. In classical statistics we have $n \geq p$ and we use an Ordinary Least Squares estimator OLS. In modern statistics we need to consider the case $n < p$ of Big Data. The OLS is then penalized. Surprising links between the pattern discovered by an estimator with a polyhedral penalty pen and the geometry of the pen^* -dual ball B^* will be explained.

Plan of the lectures: 1. OLS Estimator. 2. LASSO Estimator and its properties.
3. Estimators with a polyhedral penalty and their properties.



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